

**The 12th International Conference on
Development and Application Systems
DAS 2014**

**May 15-17, 2014
Suceava - Romania**

www.dasconference.ro

Conference Program

Organized by

**Stefan cel Mare University of Suceava
Faculty of Electrical Engineering
and Computer Science**

With technical sponsorship from

**IEEE Industry Applications Society, Romania Section
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The 12th International Conference on **Development and Application Systems (DAS)**, organized biennially by *the Faculty of Electrical Engineering and Computer Science, Ștefan cel Mare University of Suceava*, has four sections:

A - Systems, Process Control and Automations

B - Communications and Computer Networks

C - Electronics and Computer Aided Engineering

D - Software Engineering and Information Technologies

The scope of the Conference is to bring together specialists from universities, research institutes and companies for useful ideas exchanges regarding concerns in their domains. The latest progresses in these fields, as well as the newest scientific and technical results, will be presented and discussed during the Conference.

Participant registration will take place in Building D, first Floor, on May 15 between 9:00 AM and 7:00 PM and on May 16, between 8:00 AM and 9:30 AM.

CONTACT INFORMATION

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Thursday - May 15, 2014

10:00 - 10:10 Opening Ceremony

Aula, Building E

Welcome message addressed by

Valentin POPA

Rector of Ștefan cel Mare University of Suceava

Adrian GRAUR

DAS 2014 Conference Chair

10:10 - 11:30 Plenary Session 1

Aula, Building E

Keynote Address

Haptics for Industry Applications

Kouhei OHNISHI

IEEE Fellow

Department of System Design Engineering

Keio University, JAPAN

Keynote Address

*Eddy Current Nondestructive Evaluation – the
Challenge of Accurate Modeling*

Nathan IDA

IEEE Fellow

Department of Electrical and Computer Engineering

The University of Akron, USA

11:30 - 12:00 Coffee break

D101 - Building D

12:00 - 14:00 Technical Session 1

Location information on pages 8 and 11

Section A and Section B

14:00 - 15:00 Lunch break

University Restaurant

15:00 - 17:00 Technical Session 2

***Location information on pages 13 and 16
Section C and Section D***

17:00 - 17:30 Coffee break

D101 - Building D

17:30 - 18:50 Plenary Session 2

Aula, Building E

Keynote Address

*Regulation and Command Systems in Power
Converters with a Special Emphasis on the Resonant
(and Wireless Energy) Converter*

Stanimir VALTCHEV

IEEE Senior Member

Department of Electrical Engineering

Faculty of Science and Technology

Universidade Nova de Lisboa, PORTUGAL

Keynote Address

*Petri nets Modeling and Distributed Embedded
Controller Design*

Luis GOMES

Faculty of Sciences and Technology

Universidade Nova de Lisboa, PORTUGAL

20:00 - 22:00 Cocktail Party

Bradet Restaurant

Friday - May 16, 2014

10:00 - 11:20 Plenary Session 3

Aula, Building E

Keynote Address

*Are Unpaved Roads to Rome Better Than the Paved
Ones?*

Sorin D. COTOFANA

IEEE Senior Member

Department of Software and Computer Technology
Delft University of Technology, The NETHERLANDS

Keynote Address

Computer Integration of Spatially Distributed Systems

Dan Sorin NECSULESCU

Faculty of Engineering

University of Ottawa, CANADA

11:30 - 12:30 Poster Session

Aula, Building E

12:30 - 14:00 Lunch break

University Restaurant

**14:00 - 15:00 H&S 2014 Public
Presentations**

Main Hall - Building E

15:00 - 16:00 Round table

Aula, Building E

16:00 - 17:30 H&S 2014 Award Ceremony

Main Hall - Building E

18:30 - 19:30 Departure to Sucevița

Parking lot of Building A

The transport from Suceava to Sucevița will be provided by the organizers. Accommodation for the 16.05 to 17.05 night, for all DAS 2014 participants, will be at Sofia Hotel, in Sucevița.

20:00 - 22:00 Official Dinner

Sofia Hotel / Sucevița

Saturday - May 17, 2014

09:00 - 10:00 Breakfast

Sofia Hotel / Sucevița

10:00 - 14:00 Monasteries Tour

Sucevița, Putna, Forest Equestrian Park Sucevița

14:00 - 17:00 Traditional Lunch

Sofia Hotel / Sucevița

17:15 - 18:30 Departure to Suceava

Thursday - May 15, 2014

Remus Răduleț Lecture Theatre, Building D

Technical Session 1

Systems, Process Control and Automations

12:00 - 14:00 Section A

Session Co-Chairs

Kouhei OHNISHI

Department of System Design Engineering, Keio University, JAPAN

Cornel TURCU

Ștefan cel Mare University of Suceava, Romania

Vasile Gheorghită GĂITAN

Ștefan cel Mare University of Suceava, Romania

Paper ID: 11

*Embedded Networked Monitoring and Control for Renewable
Energy Storage Systems*

Grigore STAMATESCU, Iulia STAMATESCU, Nicoleta ARGHIRA,
Ioana FAGARASAN, Sergiu Stelian ILIESCU

Department of Automatic Control and Industrial Informatics
Politehnica University of Bucharest

Paper ID: 12

*PID-Controller Application in the System for Variable
Technological Process*

Simion BARANOV¹, Irina COJUHARI², Ion FIODOROV², Leonid
GORCEAC³

¹Scientific and Engineering Centre "Informinstrument", Chișinău,
Republic of Moldova

²Technical University of Moldova, Chișinău, Republic of Moldova

³State University of Moldova, Chișinău, Republic of Moldova

Paper ID: 13

Improving Interrupt Handling in the nMPRA

Nicoleta Cristina GAITAN, Vasile Gheorghita GAITAN, Elena-
Eugenia (CIOBANU) MOISUC

Ștefan cel Mare University of Suceava, Romania

Paper ID: 17

Fuzzy Decision Support System for Solar Tracking Optimization

Iulia STAMATESCU, Grigore STAMATESCU, Nicoleta ARGHIRA,
Ioana FAGARASAN, Sergiu Stelian ILIESCU

Department of Automatic Control and Industrial Informatics
Politehnica University of Bucharest

Paper ID: 29

*Real-Time Reconfiguration of Distributed Control System Based
on Hard Petri Nets*

Victor ABABIL, Viorica SUDACEVSCHI, Marin PODUBNII, Irina
COJUHARI

Technical University of Moldova, Chişinău, Republic of Moldova

Paper ID: 30

*On Quick-Change Detection based on Process Adaptive
Modelling and Identification*

Dorel AIORDACHIOAIE

Electronics and Telecommunications Department
Dunarea de Jos University of Galati

Paper ID: 32

*Experimental Analysis on a Self Excited Induction Generator for
Standalone Wind Electric Pumping Stations*

Mohamed BARARA¹, Ahmed ABOU¹, Mohamed AKHERRAZ¹,
Abderrahim BENNASSAR¹, Silviu IONITA², Emilian LEFTER²,
Bogdan ENACHE²

¹University Mohamed V Agdal, Rabat, Morocco

²Faculty of Electronics, University of Pitesti, Romania

Paper ID: 34

*Optimal Estimation of Parameters in Systems with the Phase
Space Variable Measurability*

Mykola ILASHCHUK, Eugene SOPRONIUK

Yuriy Fedkovych Chernivtsi National University, Chernivtsi, Ukraine

Paper ID: 40

*Principle of maximum to control systems with delay and change
of phase space measurability*

Tetiana HABUZA, Fedir SOPRONIUK

Yuriy Fedkovych Chernivtsi National University, Chernivtsi, Ukraine

Paper ID: 45

*Robotic Arm Control in 3D Space Using Stereo Distance
Calculation*

Roland SZABO^{1,2}, Aurel GONTEAN¹

¹ Applied Electronics Department, Politehnica University of Timișoara

² Continetal Automotive România SRL Timișoara, Romania

Thursday - May 15, 2014

Nicolae Boțan Lecture Theatre, Building D

Technical Session 1

Communications and Computer Networks

12:00 - 14:00 Section B

Session Co-Chairs

Lieven De STRYCKER

Catholic University College Ghent, Association KULeuven, Belgium

Nicolae Dumitru ALEXANDRU

Gheorghe Asachi Technical University of Iași, Romania

Alin Dan POTORAC

Ștefan cel Mare University of Suceava, Romania

Paper ID: 9

*Matlab based Platform for the Evaluation of Modulation
Techniques used in VLC*

Steven De LAUSNAY¹, Lieven De STRYCKER¹, Jean-Pierre
GOEMAERE¹, Nobby STEVENS¹, Bart NAUWELAERS²

¹Faculty of Engineering Science, DraMCo Research Group, KU Leuven,
Gent, Belgium

²Faculty of Engineering Science, TELEMIC, ESAT, KU Leuven, Leuven,
Belgium

Paper ID: 14

*Optimization of an Improved Nyquist Filter With Piece-Wise
Polynomial Frequency Characteristic*

Nicolae Dumitru ALEXANDRU¹, Alexandra Ligia BALAN²

¹Gheorghe Asachi Technical University of Iași, Romania

²Ștefan cel Mare University of Suceava, Romania

Paper ID: 20

Hardware Event Treating in nMPRA

Elena-Eugenia (CIOBANU) MOISUC, Alexandru-Bogdan

LARIONESCU, Vasile Gheorghita GAITAN

Ștefan cel Mare University of Suceava, Romania

Paper ID: 39

Sensors Network Based on Mobile Robots

Victor ABABIL, Viorica SUDACEVSCHI, Marin PODUBNII, Irina
COJUHARI

Technical University of Moldova, Chişinău, Republic of Moldova

Paper ID: 43

*Using dual priority scheduling to improve the resource
utilization in the nMPRA microcontrollers*

Nicoleta Cristina GAITAN, Lucian ANDRIES

Ştefan cel Mare University of Suceava, Romania

Paper ID: 44

Introducing aceMote: an energy efficient 32 bit mote

Andrei STAN, Nicolae BOTEZATU

Gheorghe Asachi Technical University of Iaşi, Romania

Paper ID: 48

*Evaluation of the noise effects on Visible Light Communications
using Manchester and Miller coding*

Alin-Mihai CAILEAN^{1,2}, Barthelemy CAGNEAU², Luc

CHASSAGNE², Valentin POPA¹, Mihai DIMIAN¹

¹University of Versailles Saint-Quentin, Vélizy, France

²Ştefan cel Mare University of Suceava, Romania

Paper ID: 53

*Implementation and Performance Analysis of Zero Forcing
MIMO Detection Algorithm*

Vakulabharanam RAMAKRISHNA¹, Tipparti Anil KUMAR²

¹Department of Electronics & Communication Engineering, JNTUH,
Hyderabad, India

²Department of Electronics & Communication Engineering, SR
Engineering College, Warangal, India

Paper ID: 58

*Design of a multi-input-multiple-output visible light
communication system for transport infrastructure to vehicle
communication*

Lucian-Nicolae COJOCARIU, Valentin POPA

Ştefan cel Mare University of Suceava, Romania

Thursday - May 15, 2014

Nicolae Boțan Lecture Theatre, Building D

Technical Session 2

Electronics and Computer Aided Engineering

15:00 - 17:00 Section C

Session Co-Chairs

Nathan IDA

University of Akron, USA

Constantin FILOTE

Ștefan cel Mare University of Suceava, Romania

Eugen COCA

Ștefan cel Mare University of Suceava, Romania

Paper ID: 8

*Using a Decision Tree for Real-Time Distributed Indoor
Localization in Healthcare Environments*

Jeroen WYFFELS¹, Jos De BRABANTER¹, Jean-Pierre
GOEMAERE¹, Bart NAUWELAERS¹, Lieven De STRYCKER¹, Piet
VERHOEVE², Pieter CROMBEZ²

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²Televic Healthcare, B-8870 Izegem, Belgium

Paper ID: 21

A 2.4 GHz Phase Locked Loop for a Linear Phased Antenna Array

Anneleen Van NIEUWENHUYSE¹, Frederic TORREELE¹, Jean-
Pierre GOEMAERE¹, Lieven De STRYCKER¹, Bart NAUWELAERS²

¹Faculty of Engineering Technology, KU Leuven, Gent, Belgium

²Department of Electrical Engineering, KU Leuven, Gent, Belgium

Paper ID: 35

*A Comparison between Coded-Decoded Mode Signals on
Multifunctional Registers*

Mihai TIMIS, Alexandru VALACHI, Petru CASCAVAL, Radu SILION
Gheorghe Asachi Technical University of Iași, Romania

Paper ID: 41

Size, Shape and Temperature Effects on Ferro/Antiferro-electric Hysteresis Loops from Monte Carlo Simulations on 2D Ising Model

Daniel CHIRUTA^{1,2,3}, Christian CHONG¹, Pierre-Richard DAHOO⁴,
Yasser ALAYLI¹, Mihai DIMIAN³, Jorge LINARES²

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Paper ID: 50

A Study on Light Energy Harvesting from Indoor Environment

Aurel CHIRAP, Valentin POPA, Eugen COCA, Alin Dan POTORAC
Ștefan cel Mare University of Suceava, Romania

Paper ID: 51

The temperature dependence of magnetostatic interactions in nanowire systems

Andrei DIACONU¹, Ioan DUMITRU², Alexandru STANCU²,
Leonard SPINU³

¹ Ștefan cel Mare University of Suceava, Romania

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³ Advanced Materials Research Institute, University of New Orleans, New Orleans, U.S.A.

Paper ID: 52

Multi-Inverter Six-Phase Motor Drive with Two DC Sources and Voltage Waveform Symmetries

Valentin OLESCHUK, Vladimir ERMURATSKII, Vladimir BERZAN
Academy of Sciences of Moldova, Chișinău, Republica Moldova

Paper ID: 55

LabVIEW used for Modelling of Hysteresis for Soft Magnetic Materials

Septimiu MOTOASCA

Transilvania University of Brașov, Romania

Paper ID: 64

CSLC: The Infrastructure Compiler for SoC Design

Cristian-Gyozo HABA¹, Derek PAPPAS²

¹ Gheorghe Asachi Technical University of Iași, Romania

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Paper ID: 66

*Harmonic Analysis of Power Quality Indices Based on DWT
using Three-Phase Modern Converters*

Viorel APETREI, Constantin FILOTE, Adrian GRAUR

Ștefan cel Mare University of Suceava, Romania

Thursday - May 15, 2014

Remus Răduleț Lecture Theatre, Building D

Technical Session 2

Software Engineering and Information Technologies

15:00 - 17:00 Section D

Session Co-Chairs

Hariton Nicolae COSTIN

University of Medicine and Pharmacy Iasi, Romania

Stefan Gheorghe PENTIUC

Ștefan cel Mare University of Suceava, Romania

Cristina Elena TURCU

Ștefan cel Mare University of Suceava, Romania

Paper ID: 15

*A Black Box Approach to Physical Layer Validation for 3G/4G
Base Stations*

Mihai BARBULESCU, Mihnea IONESCU, Andrei Alexandru
ENESCU

Freescale Semiconductor, Bucharest, Romania

Paper ID: 16

*Using Neural Networks for a Discriminant Speech Recognition
System*

Daniela SCHIOPU, Mihaela OPREA

Petroleum-Gas University of Ploiești

Paper ID: 24

Production Scheduling by Using ACO and PSO Techniques

Florentina Alina TOADER

Petroleum-Gas University of Ploiești

Paper ID: 26

Automatic Fury Recognition in Audio Records

Adrian CIOBANU, Mihaela LUCA, Elena MUSCA, Ioan
PAVALOI

Institute of Computer Science, Romanian Academy, Iasi, Romania

Paper ID: 27

Color Feature Vectors Based on Optimal LAB Histogram Bins

Adrian CIOBANU, Ioan PAVALOI, Mihaela LUCA, Elena MUSCA

Institute of Computer Science, Romanian Academy, Iasi, Romania

Paper ID: 47

*A Parallel Accelerated Approach of HMM Forward Algorithm for
IBM Roadrunner Clusters*

Stefania-Iuliana SOIMAN, Ionela RUSU, Stefan-Gheorghe
PENTIUC

Ștefan cel Mare University of Suceava, Romania

Paper ID: 49

*A Second Order-Cone Programming Relaxation for Facility
Location Problem*

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² Technical University of Cluj-Napoca, Cluj-Napoca, Romania

Paper ID: 54

*Organization of High-Performance Parallel-Hierarchical
Computing Processes for Classification of Laser Beam Images*

Andriy A. YAROVYY¹, Leonid I. TIMCHENKO², Nataliya I.

KOKRIATSKAIA², Svitlana V. NAKONECHNA², Maksym S.

MATEICHUK¹

¹ Vinnytsia National Technical University, Vinnytsia, Ukraine

² State University for Transport Economy and Technologies, Kyiv,
Ukraine

Paper ID: 56

From Classical Computing to Quantum Computing

Adina BARILA

Ștefan cel Mare University of Suceava, Romania

Paper ID: 57

*Romanian2SPARQL: A Grammatical Framework approach for
querying Linked Data in Romanian language*

Anca MARGINEAN, Adrian GROZA, Radu Razvan SLAVESCU,

Ioan Alfred LETIA

Technical University of Cluj-Napoca, Cluj-Napoca, Romania

Paper ID: 60

*Spectral Analysis of Fetal Heart Rate Variability Associated with
Fetal Acidosis and Base Deficit Values*

Cristian ROTARIU, Alexandru PASARICA, Hariton COSTIN,

Dragos NEMESCU

Grigore T. Popa University of Medicine and Pharmacy, Faculty of
Medical Bioengineering, Iași, Romania

From classical computing to quantum computing

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Abstract— Quantum computing is a new field of science which uses quantum phenomena to perform operations on data. The paper presents the basic theory of quantum computing and the recent results in quantum algorithm development.

Keywords—quantum computing; qubit; quantum algorithm

I. INTRODUCTION

In the last years the importance of quantum computing has significantly increased due to both continuously shrinking of the size of silicon-based integrated circuits and the results in quantum algorithm development. The Moore's Law is well known today and it says that the number of transistors on integrated circuits doubles approximately every two years. But, it cannot continue forever. In 2005 Gordon Moore noted that transistors would eventually reach the limits of miniaturization at atomic levels. Quantum computing offers a path forward by taking advantage of quantum mechanical properties. So, the rapid progress of computer science led to a corresponding evolution of computation from classical computation to quantum computation.

Quantum computing is the new field of science which uses quantum phenomena to perform operations on data. The goal of quantum computing is to find algorithms that are considerably faster than classical algorithms solving the same problem.

II. HISTORY OF QUANTUM COMPUTING

The origin of quantum computing is considered to be the Richard Feynman's idea for constructing a computer to simulate the quantum systems[1]. In his paper [2], published in 1982, Feynman argued that only a quantum computer could efficiently simulate the quantum systems. His observation led to the speculation that, in general, the computations could be done more efficiently if using the quantum mechanical effects. Paul Benioff showed that quantum computation is at least as powerful as classical computation [3].

In 1985 David Deutsch introduced a model for quantum computation: a quantum version of Turing machine [4]. He showed that any physical process, in principle, could be perfectly modeled by a quantum computer. Also he demonstrated that the universal quantum computer can do things that the universal Turing machine cannot.

David Deutsch invented the first quantum algorithm which solves a computational problem in a more efficient way than classical computation. In 1989, in [5], Deutsch described a second model for quantum computation: quantum circuits. He demonstrated that quantum gates can be combined to achieve

quantum computation in the same way that Boolean gates can be combined to achieve classical computation.

The Deutsch-Jozsa algorithm was designed in 1992 [1] and showed the computational advantage of quantum computing over classical computing.

In 1994, Peter Shor described a polynomial time quantum algorithm for factoring integers [6] and in 1996 Lov Grover invented the quantum database search algorithm [7].

From this year, the research in quantum computing field has accelerated, computer scientists trying to build quantum computers and find other quantum algorithms.

III. BASIC CONCEPTS

A. Qubits

The fundamental unit of quantum information is called quantum bit or qubit [8]. A qubit can exist in a state corresponding to the logical state 0 or 1 as in a classical bit. These states, written $|0\rangle$ and $|1\rangle$, are called basis states. Unlike the classical bit, the general state of a qubit is a linear combination - or a superposition- of states $|0\rangle$ and $|1\rangle$:

$$|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle \quad (1)$$

The amplitudes α and β are complex numbers and they have to satisfy the relation:

$$|\alpha|^2 + |\beta|^2 = 1 \quad (2)$$

In other words, a qubit can exist as a zero, a one, or simultaneously as both 0 and 1 (when both α and β are non-zero).

A system consisting of n qubits has 2^n basis states, written $|0 0 \dots 0\rangle, \dots, |1 1 \dots 1\rangle$. The general state of an n -qubit system is a superposition of all 2^n basis states:

$$|\psi\rangle = \sum_{k=0}^{2^n-1} c_k |k\rangle \quad (3)$$

where:

$$|k\rangle = |k_{n-1}\rangle \dots |k_1\rangle |k_0\rangle \quad (4)$$

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with $|k_j\rangle$ representing the state of qubit j . The amplitudes must satisfy:

$$\sum_{k=0}^{2^n-1} c_k |k\rangle = 1 \quad (5)$$

Like the single-qubit system, a n -qubit register can store simultaneously all basic states.

B. Quantum gates

Evolution of a quantum system can be described by a unitary transformation U . A unitary transformation that acts on a small number of qubits is called a gate, in analogy to classical logic gates. Unlike the logic gates, a quantum gate has the same number of inputs and outputs. A one-qubit elementary gate is described by a 2×2 matrix:

$$U = \begin{pmatrix} a & b \\ c & d \end{pmatrix} \quad (6)$$

which transforms $|0\rangle$ into $a|0\rangle + b|1\rangle$ and $|1\rangle$ into $c|0\rangle + d|1\rangle$.

One-qubit elementary gates:

- Hadamard gate

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \quad (7)$$

- Pauli gates

$$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \quad Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \quad (8)$$

- Phase shift gates

$$R_\theta = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\theta} \end{pmatrix} \quad (9)$$

Two-qubit elementary gates:

Controlled-NOT (CNOT) gate is the quantum generalization of the XOR classical gate. It has two input qubits, the control and the target qubit. The target qubit is flipped only if the control qubit is set to 1.

$$CNOT = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \quad (10)$$

Generally, if U is a one-qubit gate with matrix representation

$$U = \begin{pmatrix} x_{00} & x_{01} \\ x_{10} & x_{11} \end{pmatrix} \quad (11)$$

then the controlled- U is a two-qubit gate with matrix representation:

$$C(U) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & x_{00} & x_{01} \\ 0 & 0 & x_{10} & x_{11} \end{pmatrix} \quad (12)$$

The first qubit is the control qubit.

The SWAP gate is the quantum generalisation of the CROSSOVER classical gate. It swaps the quantum states of two qubits.

$$SWAP = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (13)$$

The Cph (controlled phase) gate acts on two qubits and it has no classical equivalent.

$$U_{cph}(\phi) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \exp(i\phi) \end{pmatrix} \quad (14)$$

C. Measurement

Measurement is the only nonreversible operation which can be applied to a quantum state. Measurement collapses a quantum state into one of the possible basis states, so measurement is a destructive operation. If a qubit is in the state $|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle$ and a measure is performed, it obtains 0 with probability α^2 (the state of qubit become $|0\rangle$) and 1 with probability β^2 (the state of qubit become $|1\rangle$).

D. Quantum parallelism

Quantum parallelism arises from the fact that the qubit exists in multiple states simultaneously. Due to the superposition principle and the linearity of operations, a quantum computer is able to evaluate a function for many

inputs simultaneously. The term was coined by David Deutsch [4], so as to distinguish it from classical parallel computation in standard computers. He presented an example which showed that a single quantum computation may suffice to state whether a function is constant or not. Given an unknown one-bit function $f: \{0,1\} \rightarrow \{0,1\}$, Deutsch algorithm decides if f is constant or balanced in a single quantum computation. The quantum circuit looks like in Fig.1.

U_f transformation is defined by:

$$U_f |x\rangle |y\rangle = |x\rangle |y \oplus f(x)\rangle \quad (15)$$

The quantum states are:

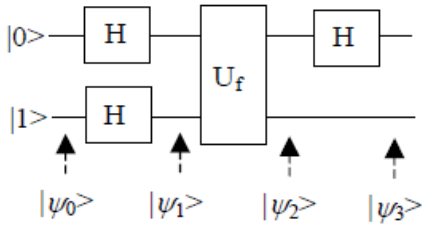


Fig. 1 - Deutsch circuit

$$|\Psi_0\rangle = |0\rangle |1\rangle \quad (16)$$

$$|\psi_1\rangle = H|0\rangle H|1\rangle$$

$$\begin{aligned} &= \left(\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle \right) \left(\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle \right) \\ &= \frac{1}{2}|0\rangle(|0\rangle - |1\rangle) + \frac{1}{2}|1\rangle(|0\rangle - |1\rangle) \end{aligned} \quad (17)$$

$$|\psi_2\rangle = U_f |\psi_1\rangle \quad (18)$$

$$\begin{aligned} &= \left(\frac{1}{\sqrt{2}}(-1)^{f(0)}|0\rangle + \frac{1}{\sqrt{2}}(-1)^{f(1)}|1\rangle \right) \left(\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle \right) \\ &= (-1)^{f(0)} \frac{1}{\sqrt{2}}(|0\rangle + (-1)^{f(0) \oplus f(1)}|1\rangle) \left(\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle \right) \end{aligned}$$

The last qubit is ignored. The Hadamard transformation transforms the state of the first qubit into:

$$(-1)^{f(0)} |f(0) \oplus f(1)\rangle$$

$f(0) \oplus f(1) = 0$ if and only if $f(0)=f(1)$ and $f(0) \oplus f(1) = 1$ if and only if $f(0) \neq f(1)$. So, when we measure 0, f is certainly constant and when we measure 1, f is balanced.

Deutsch showed that a quantum algorithm can evaluate $f(0) \oplus f(1)$ without compute $f(0)$ and $f(1)$.

Although a quantum computer can perform massive parallel computations, to compute a function simultaneously on many inputs, measurement collapses the superposition of all those states in one of the basis states.

IV. QUANTUM ALGORITHMS

A. Grover algorithm

In 1996 Lov Grover presented an algorithm for solving follow problem [7]: "Let a system have $N = 2^n$ states which are labelled S_1, S_2, \dots, S_N . These 2^n states are represented as n bit strings. Let there be a unique state, say S_n , that satisfies the condition $C(S_n) = 1$, whereas for all other states S , $C(S) = 0$ (assume that for any state S , the condition $C(S)$ can be evaluated in unit time). The problem is to identify the state S_n ." In other words, he presented an algorithm for searching an object in an unsorted list with N objects. In classical computation, searching an unsorted database cannot be done in less than linear time. Grover's algorithm has complexity $O(N^{1/2})$.

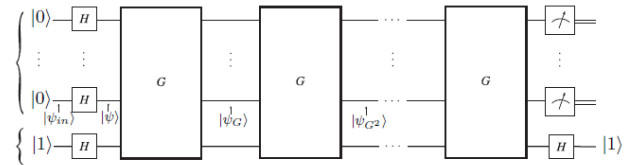


Fig. 2 - Grover circuit [9]

The circuit for implementing search has two registers: the first register has n qubits and is initialized in the state $|00\dots 00\rangle$, the last has one qubit initialized in the state $|1\rangle$.

$$|\psi_1\rangle = (H^{\otimes n} \otimes H)|0\rangle_n |1\rangle$$

$$= \frac{1}{\sqrt{2}} \sum_{x=0}^{2^n-1} |x\rangle_n (|0\rangle - |1\rangle) / \sqrt{2} = |\psi\rangle (|0\rangle - |1\rangle) / \sqrt{2} \quad (19)$$

where

$$|\psi\rangle = \frac{1}{\sqrt{N}} \sum_{x=0}^{N-1} |x\rangle_n \quad (20)$$

The Grover iteration (G) consists of two transformations:

- the first transformation marks the searched element

- the second transformation increases the probability amplitude of searched quantum state

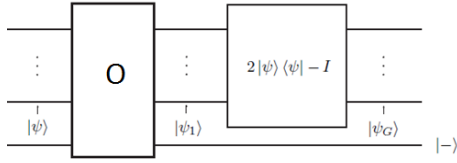


Fig. 3 - First Grover iteration [9]

The unitary transformation is called “oracle” and is defined by:

$$O|x\rangle_n|y\rangle = |x\rangle_n|y \oplus f_0(x)\rangle \quad (21)$$

where

- $|x\rangle$ is a state of the first register ($x \in \{0, 1, \dots, 2^n-1\}$)
- $|y\rangle$ is a state of the second register ($y \in \{0,1\}$)
- f is a boolean function, $f: \{0,1\}^n \rightarrow \{0,1\}$, $f_0(x)=1$ if $x=x_0$ is the searched element, $f_0(x)=0$, otherwise.

$$|\psi_1\rangle = \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} (-1)^{f(x)} |x\rangle \quad (22)$$

After O is applied the first register state is a superposition of all the basis states, but the amplitude of searched element is negative while all others are positive.

The second transformation is $2|\psi\rangle\langle\psi|-I$ and is called inversion about the mean [9] or diffusion operator. After this transformation the first register state becomes

$$|\psi_G\rangle = \frac{2^{n-2}-1}{2^{n-2}} \cdot \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} x + \frac{2}{\sqrt{2^n}} |x_0\rangle \quad (23)$$

The amplitude of the searched element increased with $O(1/N^{1/2})$, while the amplitude of unmarked states decreased.

The Grover operator is performed $\text{round}(\frac{\pi}{4}\sqrt{N})$ times

and then a measurement is performed. The outcome will be the searched value with probability approaching 1

B. Shor algorithm

In 1994 Peter Shor [6] [10] invented a quantum algorithm for solving the problem: given a composite $N \in \mathbb{N}$, determine the prime factor of N . His algorithm is used for numbers

which are not prime, even or power of prime numbers. For such number there are efficient classical algorithms.

The algorithm is as follows:

1. choose a random $x < N$
2. compute $\text{gcd}(x, N)$
3. if $\text{gcd}(x, N) \neq 1$ then there is a nontrivial factor of N and the algorithm ends
4. if $\text{gcd}(x, N) = 1$, find the order r of x (modulo N)
5. if r is even, compute $\text{gcd}(x^{r/2} \pm 1, N)$. Since $(x^{r/2}-1)(x^{r/2}+1) = x^r-1 \equiv 0 \pmod{N}$, $\text{gcd}(x^{r/2}-1, N)$ and $\text{gcd}(x^{r/2}+1, N)$ are factors of N and the algorithm ends
6. if r is odd, go to step 1

The order of x modulo N is the smallest positive integer r for which $x^r \equiv 1 \pmod{N}$. The algorithm presented by Shor reduces the factoring problem to the order-finding problem for which there isn't an efficient classical algorithm. The quantum algorithm to compute the order has the following circuit:

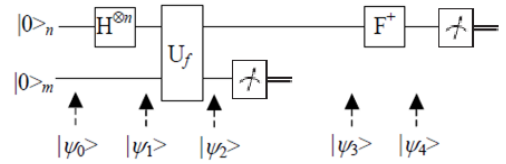


Fig. 4 - Shor circuit [10]

where U_f is the unitary operator

$$U_f(|j\rangle_n |k\rangle_m) = |j\rangle_n |x^j \bmod N\rangle_m \quad (24)$$

The first register has n qubits ($N^2 \leq 2n < 2N^2$). If r is the power of 2 then $m=n$.

The states are as following:

$$|\psi_0\rangle = |0\rangle_n |0\rangle_m \quad (25)$$

$$|\psi_1\rangle = H^{\otimes n} |0\rangle_n |0\rangle_m = \frac{1}{\sqrt{2^n}} \sum_{j=0}^{2^n-1} |j\rangle_n |0\rangle_m \quad (26)$$

$$\begin{aligned} |\psi_2\rangle &= U_f |\psi_1\rangle = \frac{1}{\sqrt{2^n}} \sum_{j=0}^{2^n-1} U_f(|j\rangle_n |0\rangle_m) \\ &= \frac{1}{\sqrt{2^n}} \sum_{j=0}^{2^n-1} |j\rangle_n |x^j \bmod N\rangle_m \end{aligned} \quad (27)$$

Since $x^j \equiv x^{j+r} \pmod N$, the function $f(x,j) = x^j \pmod N$ is periodic and has the period r .

$$\begin{aligned} |\psi_2\rangle &= \frac{1}{\sqrt{2^n}} \sum_{b=0}^{r-1} \sum_{a=0}^{2^n/r-1} |ar+b\rangle_n |x^{ar+b} \pmod N\rangle_m \\ &= \frac{1}{\sqrt{2^n}} \sum_{b=0}^{r-1} \sum_{a=0}^{2^n/r-1} |ar+b\rangle_n |x^b \pmod N\rangle_m \end{aligned} \quad (28)$$

A measurement is performed and, assuming it measures x^{b_0} , the quantum state becomes:

$$|\psi_3\rangle = \sqrt{\frac{r}{2^n}} \sum_{a=0}^{2^n/r-1} |ar+b_0\rangle_n |x^{b_0} \pmod N\rangle_m \quad (29)$$

$$\begin{aligned} |\psi_4\rangle &= F^+ |\psi_3\rangle = \sqrt{\frac{r}{2^n}} \sum_{a=0}^{2^n/r-1} F^+ |ar+b_0\rangle_n |x^{b_0} \pmod N\rangle_m \\ &= \frac{1}{\sqrt{r}} \left[\sum_{j=0}^{2^n-1} S_j e^{-\frac{2\pi i j b_0}{2^n}} |j\rangle_n \right] |x^{b_0} \pmod N\rangle_m \end{aligned}$$

$$|\psi_4\rangle = \frac{1}{\sqrt{r}} \left[\sum_{k=0}^{r-1} e^{-\frac{2\pi i k b_0}{r}} \left| \frac{k \cdot 2^n}{r} \right\rangle_n \right] |x^{b_0} \pmod N\rangle_m \quad (30)$$

Measuring the first register, we get the value $m=k_0 2^n/r$, where k_0 can be any value between 0 and $r-1$ with equal probability. If $m=0$, the algorithm must be run again. If $m \neq 0$, using classical algorithms, the rational value of k_0/r is obtained. The denominator of this value is the searched order of x .

V. PROGRESS IN QUANTUM ALGORITHMS

The two quantum algorithms invented by Grover and Shor have remained the most spectacular quantum algorithms. In the last years many quantum algorithms have been developed but they are generalisations and applications of the two results.

Boyer, Brassard, Høyer and Tapp [11][12] generalized Grover's algorithm for the case N isn't a power of 2. Also, they generalised the algorithm for the case when the search problem has t solutions (t known and $t \neq 0$), finding one values in $\text{round}\left(\frac{\pi}{4} \sqrt{\frac{N}{t}}\right)$ iterations. Another generalisation was done by Long, Li, Zhang și Niu [13] who replaced Grover operators by arbitrary unitary and arbitrary phase rotation

operators. Ashley Montanaro observed that in real life it is rarely necessary to search in a completely unstructured database, so he considered the problem of search when it is given an advice as to where the marked element might be located. The "advice" is a probability distribution $\mu = (p_y)$, $y \in \{1, \dots, n\}$, where p_y is the probability that $f(y)=1$ [14]. André J. Hoogstrate and Chris A.J. Klaassen showed that Montanaro's algorithm can speed up the search within a finite population for a single particular individual or item with rare characteristic [15]. This is very useful for optimizing security screening applications.

Brassard, Hoyer and Tapp [16] developed a quantum algorithm to solve the of counting the number of elements that satisfy some conditions instead of finding such an element. Their algorithm uses both Grover's iteration and the quantum Fourier transform.

Based on the generalized search algorithm, Dürr and Høyer [17] gave a quantum algorithm for finding the minimum in an unsorted list with $O(N^{1/2})$ complexity. Ahuja and Kappor [18] presented a quantum algorithm for finding maximum in an unsorted list.

Many applications of quantum algorithms have been developed in the graphs field. Dürr, Heiligman, Hoyer and Mhalla [19] presented some quantum algorithms for connectivity, minimum spanning tree and the single source shortest path. They showed that the algorithm for finding a minimum spanning tree has $O(n^{3/2})$ complexity in the matrix model and $O(\sqrt{nm})$ complexity in the adjacency list model. (where n is the number of vertices and m is the number of edges). The query complexity of single source shortest path algorithm is $O(n^{3/2} \log^2 n)$ in the matrix model and $O(\sqrt{nm})$ in the adjacency list model. The complexity of the connectivity algorithm is $O(n^{3/2})$ in the matrix model. In the adjacency list model, the complexity is $O(n)$ for undirected graphs, respectively $O(\sqrt{nm})$ for directed graphs.

Magniez, Santha and Szegedy [20] presented two algorithms for finding a triangle in a n -vertex undirected graph. The first uses quantum search and gives the result in $O(n^{10/7})$ queries. The second is based on quantum walks and gives the result in $O(n^{13/10})$ queries. A. Belovs [21] designed a quantum algorithm for the triangle problem with $O(n^{35/27})$ query complexity. In 2013, Lee, Magniez and Santha [22] developed a better algorithm, with $O(n^{9/7})$ query complexity.

In 2007, Sebastian Dörn studied the graph traversal problem on quantum computers. In his paper [23], Dörn showed that the algorithm for Eulerian graph problem has a $O(\sqrt{n})$ query complexity in the adjacency list model and $O(n^{1.5})$ query complexity in matrix model. The quantum query complexity of Hamiltonian circuit algorithm is $O(n^{2n/(n+1)})$ in the matrix model.

The graph collision problem was studied by Magniez, Santha and Szegedy in [20]. Their algorithm has $O(n^{2/3})$ complexity. For some classes of graphs there are better algorithms. So, Jeffrey, Kothari Magniez described in [24] a quantum algorithm with $\tilde{O}(\sqrt{n} + \sqrt{m})$ query complexity,

where m is the number of non-edges in the graph. Belov's algorithm has $O(n^{1/2}\alpha^{1/6})$ query complexity, where α is the size of the largest independent set of the graph [25][26]. The algorithm described by Ambainis et al. [26] has $O(n^{1/2}t^{1/6})$ query complexity, where t is the treewidth of the graph.

In 2009, Harrow, Hassidim and Lloyd produced a quantum algorithm for solving systems of linear equations in time $O(k^2 \log N)$ where k is the condition number of the system of equations [27]. In 2012, Andris Ambainis improved the running time of the algorithm of Harrow to $O(k \log^3 k \log N)$ [28]. Their algorithms are used by Dominic Berry to develop a quantum algorithm for solving linear differential equations [29].

VI. CONCLUSIONS

Quantum computing permits to perform computational operations on data much faster and efficiently by taking advantage of quantum parallelism. At the same time, by using the principle of superposition, a large amount of data could be stored.

In the last years, a lot of quantum algorithms have been developed. Many of them are generalisations and applications of the two main algorithms – Shor's factoring algorithm and Grover's search algorithm. The paper presented some of the the recent results in the quantum algorithm development focusing on the quantum search algorithm. These algorithms use the techniques of the quantum search to solve problems faster than their classical counterparts can do.

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